

# The Sieve of Eratosthenes: Primes and Composites

## Unit: Number Play - Student Practice Worksheet

*Overview: Kabir tried to list every prime number from 1 to 100 by testing each one for factors, one at a time. Forty minutes in, he had checked eleven numbers and made three mistakes already. Ms. Rao handed him a grid and a pencil and said, "Cross out numbers instead of testing them. You'll be done in five minutes."*

### Practice Questions (30 Total)

#### Section A - Easy

**Q1. The chips show every factor of 7. How many factors does this prime have?**

Factors of 7

1

7

no other chips

- ☐ A. 2
- ☐ B. 1
- ☐ C. 3
- ☐ D. It varies

**Q2. Is 1 a prime number?**

- ☐ A. Yes
- ☐ B. No
- ☐ C. Only sometimes
- ☐ D. Only if doubled

**Q3. Which of these is a prime number?**

- ☐ A. 9
- ☐ B. 15
- ☐ C. 7
- ☐ D. 21

**Q4. The strip shows what happens right after 2 is circled. What happens to the later evens?**



After circling 2, every later even is crossed

- ☐ A. They stay circled as primes
- ☐ B. They are ignored
- ☐ C. They are divided by 3
- ☐ D. They are crossed out as multiples of 2

**Q5. How many factors does a prime number have?**

- ☐ A. Exactly two: 1 and itself
- ☐ B. Exactly one
- ☐ C. Three or more
- ☐ D. It varies with size

**Q6. Which of these is a composite number?**

- ☐ A. 13
- ☐ B. 12
- ☐ C. 11
- ☐ D. 17

**Q7. The grey box is crossed out before any circling starts. Which special number is that?**



then 2, 3, 4, 5...

- ☐ A. 0
- ☐ B. 2
- ☐ C. 1
- ☐ D. 100

**Q8. Kabir wrongly called 21 a prime number. What was his mistake?**

- ☐ A. 21 actually has no factors
- ☐ B. 21 is smaller than 20
- ☐ C. 21 is an even number
- ☐ D. He forgot 21 divides evenly by 7

**Q9. What is the smallest prime number?**

- ☐ A. 0
- ☐ B. 1
- ☐ C. 3
- ☐ D. 2

**Q10. What is the name of the method that finds primes by crossing out multiples?**

- ☐ A. The prime testing rule
- ☐ B. The Sieve of Eratosthenes
- ☐ C. The factor tree
- ☐ D. The number line method

### Section B - Medium

**Q11. After crossing multiples of 2 and 3, which remaining number in the strip is the next prime to circle?**

|   |   |    |    |    |    |
|---|---|----|----|----|----|
| 2 | 3 | 4  | 5  | 6  | 7  |
| 8 | 9 | 10 | 11 | 12 | 13 |

- ☐ A. 5
- ☐ B. 9
- ☐ C. 4
- ☐ D. 12

**Q12. Why does crossing out multiples of 2, then 3, then 5, then 7 already catch every composite number up to 100?**

- ☐ A. Because 100 is itself prime

- ☐ B. Because only even numbers can be composite
- ☐ C. Because any composite up to 100 must have a prime factor of 10 or less
- ☐ D. It's a coincidence with no real reason

**Q13. How many prime numbers are there between 1 and 20?**

- ☐ A. 6
- ☐ B. 8
- ☐ C. 7
- ☐ D. 9

**Q14. Among these four cards, which multiple of 3 would the sieve cross out first?**



- ☐ A. 11
- ☐ B. 13
- ☐ C. 15
- ☐ D. 9

**Q15. 37 survives every round of crossing out in a sieve of 1-50. What does this tell you?**

- ☐ A. 37 must be prime
- ☐ B. 37 must be composite
- ☐ C. 37 must be equal to 1
- ☐ D. Nothing can be concluded

**Q16. A number has factors 1, 2, 4, 8, and 16. Is it prime or composite?**

- ☐ A. Prime, since it starts and ends with 1 and itself
- ☐ B. Composite, since it has more than two factors
- ☐ C. Neither, since it's a power of 2
- ☐ D. Cannot be determined

**Q17. Which pair of circled numbers on this strip are both prime?**



- ☐ A. 15 and 16
- ☐ B. 18 and 20
- ☐ C. 17 and 19
- ☐ D. 16 and 18

**Q18. In the sieve method, once you've crossed out multiples of 2, 3, 5, and 7 up to 100, do you need to check multiples of 11 too?**

- ☐ A. Yes, always
- ☐ B. Only for odd numbers
- ☐ C. Only if 11 is composite
- ☐ D. No, since  $11 \times 11$  exceeds 100

**Q19. Which of these numbers is composite but NOT a multiple of 2 or 3?**

- ☐ A. 14
- ☐ B. 27
- ☐ C. 25
- ☐ D. 18

**Q20. How many composite numbers are there between 2 and 10 inclusive?**

- ☐ A. 3
- ☐ B. 5
- ☐ C. 4
- ☐ D. 6

### Section C - Challenge

**Q21. On this 90s strip, which single circled number survives a full sieve?**

91

93

95

97

99

 $91=7\times 13$ ,  $93=3\times 31$ ,  $95=5\times 19$ ,  $99=9\times 11$ 

- ☐ A. 97
- ☐ B. 93
- ☐ C. 99
- ☐ D. 91

**Q22. Which statement correctly compares the sieve method to Kabir's original one-by-one testing approach?**

- ☐ A. Both methods are equally fast
- ☐ B. The sieve avoids repeated division testing by reusing earlier crossing-out work
- ☐ C. One-by-one testing is always more accurate
- ☐ D. The sieve only works for numbers under 20

**Q23. A sieve up to 30 crosses out 1, then multiples of 2, 3, and 5. Which number is the LARGEST that survives?**

- ☐ A. 27
- ☐ B. 29
- ☐ C. 28
- ☐ D. 25

**Q24. When sieving multiples of 5, why does the highlighted 25 come before any still-open multiple of 5?**

10

15

20

25

10, 15, 20 were already multiples of 2 or 3

- ☐ A. Because 10 is not a real number
- ☐ B. Because 5 has no smaller multiples
- ☐ C. Because 10, 15, 20 were already crossed out as multiples of 2 or 3
- ☐ D. There is no real reason — starting point doesn't matter

**Q25. A number less than 100 has exactly 3 distinct prime factors. Can it still be found by a standard sieve of 1-100?**

- ☐ A. No, the sieve only works for numbers with 2 prime factors
- ☐ B. No, such numbers are always prime
- ☐ C. Only if all three factors are the same
- ☐ D. Yes — the sieve marks ALL composites, regardless of how many distinct prime factors they have

**Q26. In a sieve of 1-100, which round of crossing-out eliminates the number 91?**

- ☐ A. The multiples-of-7 round, since  $91=7\times 13$
- ☐ B. The multiples-of-2 round
- ☐ C. The multiples-of-3 round
- ☐ D. 91 is never eliminated — it's prime

**Q27. If the sieve skips the multiples-of-3 round, what happens to the peach cells?**



Peach cells would stay wrongly uncrossed

- ☐ A. Real primes like 7 get crossed out by mistake
- ☐ B. The number 11 becomes composite
- ☐ C. Composites like 9 and 21 stay wrongly uncrossed as if prime
- ☐ D. Nothing changes at all

**Q28. A student says the sieve proves there are only a limited number of primes, since eventually everything gets crossed out. Is this reasoning sound?**

- ☐ A. Yes, the sieve proves primes are finite
- ☐ B. Yes, but only for even limits
- ☐ C. The sieve is unrelated to primes
- ☐ D. No, the sieve just has a chosen limit

**Q29. Anaya wants to extend a sieve from 1-100 to 1-200. Up to which prime must she now cross out multiples, to guarantee every composite under 200 is caught?**

- ☐ A. 7, same as before
- ☐ B. 13, since its square is just under 200

- ☐ C. 19, to be extra safe
- ☐ D. 100, half of 200

**Q30. Kabir's one-by-one testing missed 21 as composite. Which sieve flaw would cause a similar miss?**

- ☐ A. Stopping the crossing-out rounds too early, before reaching a prime whose square is still under the limit
- ☐ B. The sieve has no possible flaw ever
- ☐ C. Crossing out too many numbers by mistake
- ☐ D. Starting the sieve at 0 instead of 1

## Answer Key

**Q1:** (A) (a) 2. The diagram has exactly two chips, 1 and 7 — that is the definition of a prime.

**Q2:** (B) (b) No. 1 has only one factor, itself, so it is neither prime nor composite.

**Q3:** (C) (c) 7. 7's only factors are 1 and 7. The others all have more than two factors —  $9=3\times3$ ,  $15=3\times5$ ,  $21=3\times7$ .

**Q4:** (D) (d) They are crossed out as multiples of 2. Circling 2 marks it prime; every later even is a multiple and must go.

**Q5:** (A) (a) Exactly two: 1 and itself. More than two factors would make the number composite.

**Q6:** (B) (b) 12. 12 has factors 1, 2, 3, 4, 6, and 12 — more than two. The others are all prime.

**Q7:** (C) (c) 1. Since 1 is neither prime nor composite, it is crossed out at the very start.

**Q8:** (D) (d) He forgot 21 divides evenly by 7.  $21=3\times7$ , giving it more than two factors, so it is composite.

**Q9:** (D) (d) 2. 2 is the smallest, and only even, prime — every other even number is divisible by 2.

**Q10:** (B) (b) The Sieve of Eratosthenes. Named after the ancient Greek mathematician who devised this crossing-out method.

**Q11:** (A) (a) 5. 4, 6, 8, 9, 10, 12 are already crossed. 5 is the smallest uncrossed number after 2 and 3.

**Q12:** (C) (c) Because any composite up to 100 must have a prime factor of 10 or less. If both factors exceeded 10, the product would exceed 100, so sieving through 7 is enough.

**Q13:** (B) (b) 8. The primes up to 20 are 2, 3, 5, 7, 11, 13, 17, 19.

**Q14:** (D) (d) 9. The peach card 9 is the smallest multiple of 3 in the row, so it is crossed before 15.

**Q15:** (A) (a) 37 must be prime. Surviving every round of crossing-out is exactly the sieve's definition of being prime.

**Q16:** (B) (b) Composite, since it has more than two factors. Five factors automatically disqualifies it from being prime.

**Q17:** (C) (c) 17 and 19. Both are circled and uncrossed. Every other pair on the strip is already struck through.

**Q18:** (D) (d) No, since  $11\times11$  exceeds 100. Any composite multiple of 11 under 100 already has a second factor of 9 or less, caught earlier.

**Q19:** (C) (c) 25.  $25=5\times5$  is composite but not divisible by 2 or 3 — it only gets crossed out in the multiples-of-5 round.

**Q20:** (B) (b) 5. From 2 to 10, the composites are 4, 6, 8, 9, and 10, while 2, 3, 5, 7 are prime.

**Q21:** (A) (a) 97. The caption already factors the struck numbers:  $91=7\times13$ ,  $93=3\times31$ ,  $95=5\times19$ ,  $99=9\times11$ .

**Q22:** (B) (b) The sieve avoids repeated division testing by reusing earlier crossing-out work. Once a number is crossed out, it never needs to be tested again.

**Q23:** (B) (b) 29.  $27=3\times 9$  and  $25=5\times 5$  get crossed out, 28 is even, and 29 has no factors besides 1 and itself.

**Q24:** (C) (c) Because 10, 15, 20 were already crossed out as multiples of 2 or 3. 25 is the first multiple of 5 with no smaller prime factor.

**Q25:** (D) (d) Yes — the sieve marks ALL composites, regardless of how many distinct prime factors they have.

**Q26:** (A) (a) The multiples-of-7 round, since  $91=7\times 13$ . 91 is odd and not divisible by 3 or 5, so it survives until 7.

**Q27:** (C) (c) Composites like 9 and 21 stay wrongly uncrossed as if prime. Skipping a round never falsely crosses out a real prime.

**Q28:** (D) (d) No, the sieve just has a chosen limit. Finding a fixed count in 1-100 says nothing about primes beyond 100.

**Q29:** (B) (b) 13, since its square is just under 200.  $13\times 13=169$  is under 200, but  $17\times 17=289$  exceeds it.

**Q30:** (A) (a) Stopping the crossing-out rounds too early. If you stop after only 2 and 3, composites like 25 or 49 would wrongly survive.

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